

**LESSON**  
**7-1**

**Finding Rational Solutions of Polynomial Equations**

*Practice and Problem Solving*

Solve each polynomial equation by factoring.

1.  $4x^3 + x^2 - 4x - 1 = 0$

2.  $x^5 - 2x^4 - 24x^3 = 0$

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3.  $3x^5 + 18x^4 - 21x^3 = 0$

4.  $-x^4 + 2x^3 + 8x^2 = 0$

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Identify the rational zeros of each function. Then write the function in factored form.

5.  $f(x) = x^3 + 3x^2 + 3x + 1$

6.  $f(x) = x^3 + 5x^2 - 8x - 48$

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Identify all the rational roots of each equation.

7.  $x^3 + 10x^2 + 17x = 28$

8.  $3x^3 + 10x^2 - 27x = 10$

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**Solve.**

9. An engineer is designing a storage compartment in a spacecraft. The compartment must be 2 meters longer than it is wide, and its depth must be 1 meter less than its width. The volume of the compartment must be 8 cubic meters.

a. Write an equation to model the volume of the compartment.

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b. List all possible rational roots. \_\_\_\_\_

c. Use synthetic division to find the roots of the polynomial equation. Are the roots all rational numbers?

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d. What are the dimensions of the storage compartment? \_\_\_\_\_

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**Finding Rational Solutions of Polynomial Equations**

*Practice and Problem Solving*

Solve each polynomial equation by factoring.

10.  $-3x^4 + 6x^3 + 105x^2 = 0$

11.  $8x^7 - 56x^6 + 96x^5 = 0$

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Identify the rational zeros of each function. Then write the function in factored form.

12.  $f(x) = x^3 + 6x^2 + 12x - 8$

13.  $f(x) = x^3 + 10x^2 + 32x + 32$

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Identify all the rational roots of each equation.

14.  $x^3 + 2x^2 - 48x = 0$

15.  $5x^4 + 19x^3 - 29x^2 + 5x = 0$

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16.  $6x^3 + 12x^2 - 18x = 0$

17.  $3x^4 + 5x^3 - 11x^2 + 3x = 0$

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**Solve.**

18. A jewelry box is designed such that its length is twice its width and its depth is 2 inches less than its width. The volume of the box is 64 cubic inches.

a. Write an equation to model the volume of the box.

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b. List all possible rational roots. \_\_\_\_\_

c. Use synthetic division to find the roots of the polynomial equation. Are the roots all rational numbers?

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d. What are the dimensions of the box? \_\_\_\_\_